## Show all work that leads to your answers!

## 1.

Let $f(x)=e^{2 x}$. Let $R$ be the region in the first quadrant bounded by the graph of $y=f(x)$ and the vertical line $x=1$, as shown in the figure above.
(a) Write an equation for the line tangent to the graph of $f$ at $x=1$.
(b) Find the area of $R$.
(c) Region $R$ forms the base of a solid whose cross sections perpendicular to the $y$-axis are squares. Write, but do not evaluate, an expression involving one or more integrals that gives the volume of the solid.


## 2.

Particle $X$ moves along the positive $x$-axis so that its position at time $t \geq 0$ is given by $x(t)=5 t^{3}-9 t^{2}+7$.
(a) Is particle $X$ moving toward the left or toward the right at time $t=1$ ? Give a reason for your answer.
(b) At what time $t \geq 0$ is particle $X$ farthest to the left? Justify your answer.
(c) A second particle, $Y$, moves along the positive $y$-axis so that its position at time $t$ is given by $y(t)=7 t+3$. At any time $t, t \geq 0$, the origin and the positions of the particles $X$ and $Y$ are the vertices of a triangle in the first quadrant. Find the rate of change of the area of the triangle at time $t=1$. Show the work that leads to your answer.

