

1.

$$(a) \int_0^{300} r(t) dt = 270$$

According to the model, 270 people enter the line for the escalator during the time interval  $0 \leq t \leq 300$ .

$$(b) 20 + \int_0^{300} (r(t) - 0.7) dt = 20 + \int_0^{300} r(t) dt - 0.7 \cdot 300 = 80$$

According to the model, 80 people are in line at time  $t = 300$ .

(c) Based on part (b), the number of people in line at time  $t = 300$  is 80.

The first time  $t$  that there are no people in line is

$$300 + \frac{80}{0.7} = 414.286 \text{ (or } 414.285) \text{ seconds.}$$

(d) The total number of people in line at time  $t$ ,  $0 \leq t \leq 300$ , is modeled by

$$20 + \int_0^t r(x) dx - 0.7t.$$

$$r(t) - 0.7 = 0 \Rightarrow t_1 = 33.013298, t_2 = 166.574719$$

$t$	People in line for escalator
0	20
$t_1$	3.803
$t_2$	158.070
300	80

The number of people in line is a minimum at time  $t = 33.013$  seconds, when there are 4 people in line.

2.

(a)  $v'(3) = -2.118$

The acceleration of the particle at time  $t = 3$  is  $-2.118$ .

(b)  $x(3) = x(0) + \int_0^3 v(t) dt = -5 + \int_0^3 v(t) dt = -1.760213$

The position of the particle at time  $t = 3$  is  $-1.760$ .

(c)  $\int_0^{3.5} v(t) dt = 2.844$  (or 2.843)

$$\int_0^{3.5} |v(t)| dt = 3.737$$

The integral  $\int_0^{3.5} v(t) dt$  is the displacement of the particle over the time interval  $0 \leq t \leq 3.5$ .

The integral  $\int_0^{3.5} |v(t)| dt$  is the total distance traveled by the particle over the time interval  $0 \leq t \leq 3.5$ .

(d)  $v(t) = x_2'(t)$

$$v(t) = 2t - 1 \Rightarrow t = 1.57054$$

The two particles are moving with the same velocity at time  $t = 1.571$  (or 1.570).

